

Concept development, floating bridge E39 Bjørnafjorden

Appendix K – Enclosure 8

10205546-13-NOT-194

Shear lag and buckling effects of Bridge Girder concept K12

MEMO

PROJECT	Concept development, floating bridge E39 Bjørnafjorden	DOCUMENT CODE	10205546-13-NOT-194
CLIENT	Statens vegvesen	ACCESSIBILITY	Restricted
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SUMMARY

When designing the bridge girder, effects of shear lag and plate buckling must be taken into account at the ultimate, serviceability and fatigue limit state. This memo presents the design requirements and the applied design approach accounting for these effects.

Sufficient capacity of the bridge girder subject to compression and biaxial bending is verified based on equation (4.15) in NS-EN 1993-1-5:2006 + NA 2009. Equation (4.15) is a linear summation of the utilization that each force component utilizes the capacity corresponding to the respective type of force. Due to the bridge girders shape with an inclined bottom plate, the capacity check will give conservative utilization results for biaxial bending when the utilization about each axis is large at the same time.

Since the Eurocode does not account for conservative utilizations due to geometric shapes, a second way of performing the capacity check has been introduced. In the second method, the geometric shape is considered in the capacity check by calculating the utilization at all the 7 extremity points of the girder based on the effective elastic section modulus for the specific point.

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1 Introduction

When designing the bridge girder, effects of shear lag and plate buckling must be taken into account at the ultimate, serviceability and fatigue limit state. This memo will present the design requirements and the applied design approach.

Calculation examples will be given, but the final results of the bridge girder capacity verification can be found in a closure to Appendix G: Global Analyses – Response, as it is a part of the post-processing routine of the global analyses results.

1.1 Design method

NS-EN 1993-1-5:2006 + NA:2009 provides two different design methods for plated steel structures; effective width method and reduced stress method. The applied method for the design of the bridge girder will be the effective width method, where all requirements are given in chapters 3 – 9 of the NS-EN 1993-1-5. The effective width method is efficient because it accounts for post-critical reserve in single plate elements and load shedding between cross-sectional elements.

Similar to the Eurocode, the following designation of three types of effective cross-section and effective width will be used in this memo:

- Effective^s – includes effects of shear lag
- Effective^p – includes effects of plate buckling
- Effective – includes effects of both shear lag and plate buckling

1.2 Bridge girder

Figure 1 to Figure 3 shows the longitudinal steel in the typical bridge girder sections at mid span and by columns. Transverse bulkheads and trusses are not shown in the figures, as their design is not within the scope of this memo.

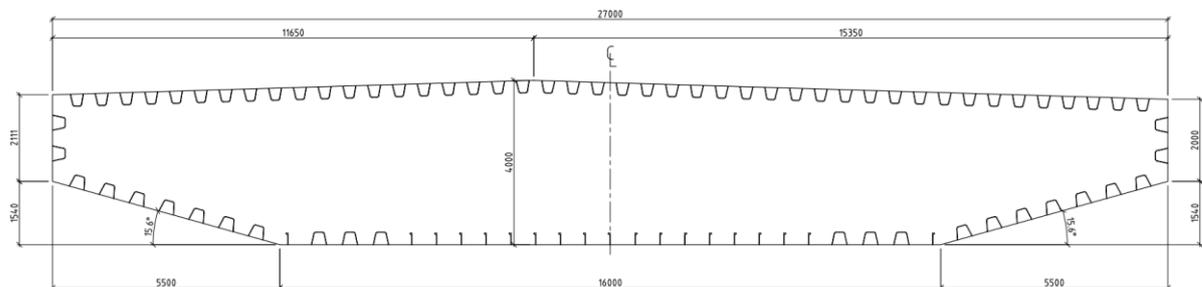


Figure 1 Bridge girder section at mid span

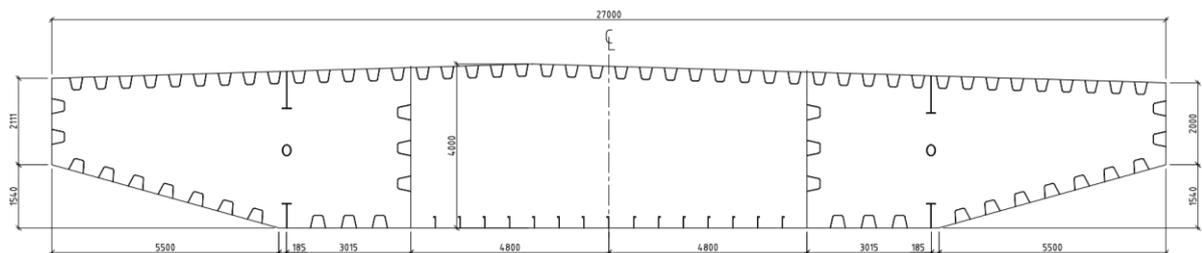


Figure 2 Bridge girder section by column axis 3 - 8

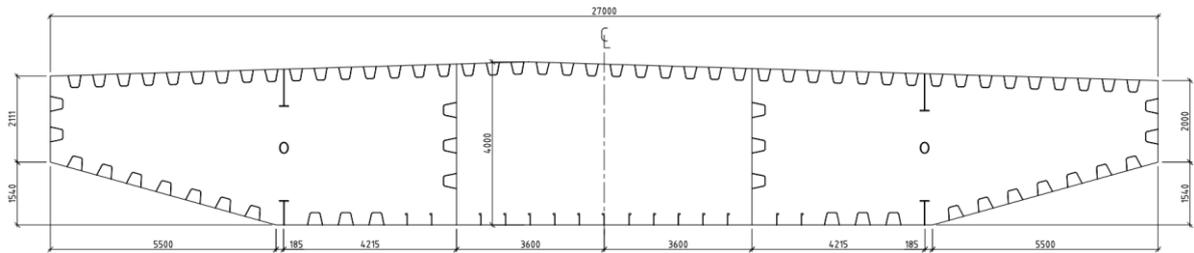


Figure 3 Bridge girder section by column axis 9 – 38

Figure 4 shows the positive direction of the v – vertical axis, h – horizontal axis and l – longitudinal axis as they are in the model for the global analysis of each bridge concept. The positive direction for the axial force, N_{Ed} , moment about the weak axis (horizontal), M_{weak} , and moment about the strong axis (vertical), M_{strong} , are also shown in the figure.

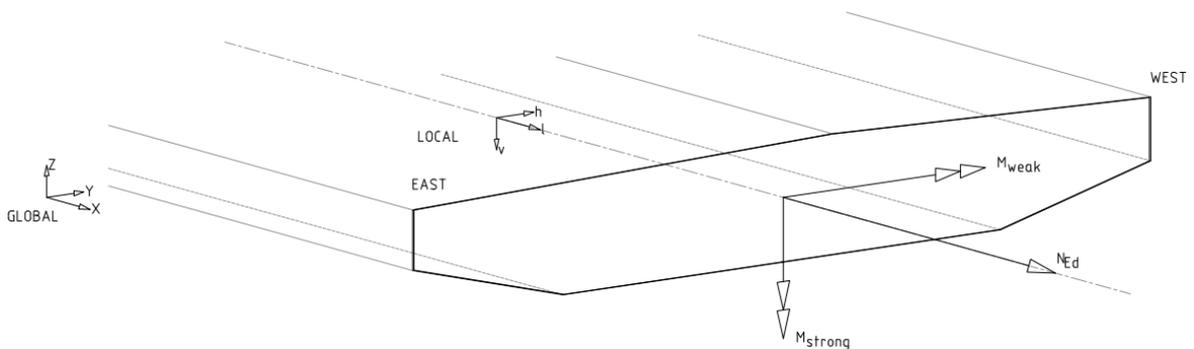


Figure 4 Local axis system in bridge girder and positive force direction

2 Design requirements

NS-EN 1993-1-5:2006 + NA:2009 (later referred to as EC3-5) gives design requirements of stiffened (and unstiffened) plates which are subject to in-plane forces.

2.1 Global analysis

According to clause 2.2(1)P in EC3-5, the effects of shear lag and of plate buckling on the stiffness of members shall be taken into account in the global analysis. Further on, in clause 2.2(5), it is stated that the effects of plate buckling on the stiffness can be ignored if the effective^p cross-sectional area of the girder in compression is larger than ρ_{lim} times the gross cross-sectional area of the girder. Clause NA.2.2(5) of the National Annex to EC3-5 gives the value of ρ_{lim} as 0.5.

2.2 Shear lag in member design

Shear lag effects are dependent on the span of the bridge, as well as the width of the internal elements in the flanges of the girder. With the typical span of Bjørnafjorden being 125 m, the distance L_e determined from Figure 3.1 in EC3-5 is 87,5 m for sagging bending, and 62,5 m for hogging bending.

According to clause 3.1(1) in EC3-5, the effects of shear lag may be neglected if half the width of the internal elements in the flanges of the girder is less than $L_e/50$. This is never the case for the bridge girder of Bjørnafjorden, hence shear lag effects should be considered at serviceability and fatigue limit state according to clause 3.2.1, and at ultimate limit state according to clause 3.3 of EC3-5.

2.3 Plate buckling effects due to direct stresses at the ultimate limit state

Sufficient capacity of the bridge girder due to direct stresses is verified based on equation (4.15) given in clause 4.6(1) in EC3-5:

$$\eta_1 = \frac{N_{Ed}}{f_y A_{eff}} + \frac{M_{y,Ed} + N_{Ed} e_{y,N}}{f_y W_{y,eff}} + \frac{M_{z,Ed} + N_{Ed} e_{z,N}}{f_y W_{z,eff}} \quad (4.15)$$

The effective cross-sectional properties of the girder are based on the effective areas of the compression elements and on the effective^s area of the tension elements due to shear lag, in accordance with clause 4.3(2).

According to clause 4.3(3) and 4.3.(4), the effective^p area A_{eff} should be determined assuming that the cross-section is subject only to stresses due to uniform axial compression. The shift, $e_{y,N}$ and $e_{z,N}$, of the centroid of the effective^p area A_{eff} relative to the center of gravity of the gross cross-section, gives an additional moment which should be taken into account in the cross-section verification. The effective section modulus W_{eff} should be determined assuming the cross-section is subject only to bending stresses about the respective axis.

2.4 Further requirements

In addition to the requirements for checking effects of shear lag and plate buckling effects due to direct stresses, NS-EN 1993-1-5:2006 + NA:2009 also gives requirements and resistance models for shear buckling and buckling due to transverse loads.

Experience shows that buckling effects due to shear loads for a heavily stiffened plated structure are very low (often neglectable), thus at this stage of design, the shear resistance is considered as full. A check of the von mises stress in the girder at ULS is performed in order to verify the capacity. Results of this check can be found in a closure to 90-RE-107 Appendix G: Global Analyses – Response_0

3 Shear lag effects

At serviceability and fatigue limit state, an effective^s width for elastic shear lag is used in accordance with clause 3.2 of EC3-5. The effective^s width is $b_{eff} = \beta b_0$, where the effective^s width factor β is calculated based on formulas given in table 3.1 of the Eurocode.

In the global analysis, the stiffness of the bridge girder about the weak axis is based on the effective^s cross-section attained by using the effective^s flange widths $b_{eff} = \beta b_0$.

Refer to memo 13-NOT-099 – FEM analysis of bridge girder and column for verification of shear lag factors calculated according to clause 3.2 of the Eurocode compared to the shear lag experienced in the local FE-model of the bridge girder.

At ultimate limit state, elastic-plastic shear lag effects are taken into account as given in clause 3.3(1)c). As the National Annex does not specify a preferred method, the recommended method in NOTE 3 is adapted. The effective^s width is $b_{eff} = \beta^k b_0$, where the factors β and k are calculated according to table 3.1 of NS-EN 1993-1-5.

The elastic-plastic shear lag effects are combined with the effects of plate buckling due to direct stresses at the ultimate limit state. This is further explained in section 4.2.4 of this memo.

An additional check of the von mises stresses at 7 extremity points of the bridge girder is performed at the ultimate limit state. For these calculations, the effective^s flange width applied when calculating the second moment of area about the weak axis is taken as $b_{eff} = b_0 \beta^k$.

3.1 Calculation example

On the following pages, examples of calculations of β and β^k factors at sagging and hogging bending are shown.

Figure 5 shows the girder section at sagging bending. Top and bottom flanges are internal flanges, and the width b_0 is half of their width. The calculations below give the β and β^k for the top and the bottom flange.

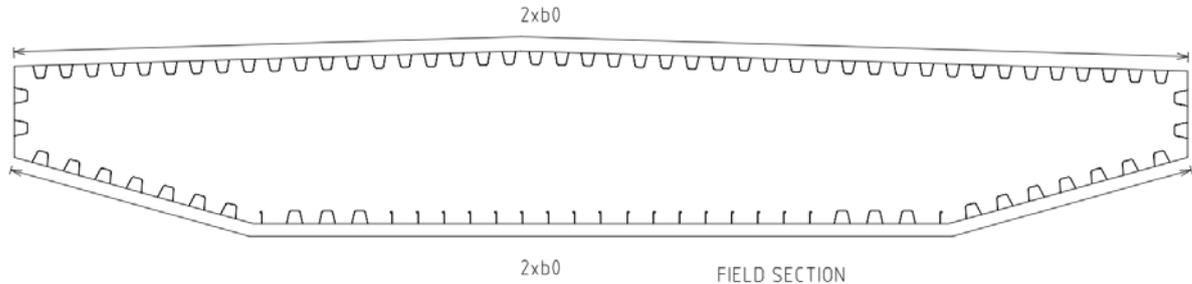


Figure 5 Section at sagging bending

NS-EN 1993-1-5 chapter 3.2 Effective^s width for shear lag and 3.3 Shear lag at the ultimate limit state

kNm := kN·m

Input

Top flange at sagging bending:

$b_0 := 13506 \cdot \text{mm}$	Half width of flange
$A_s := 5923 \text{mm}^2$	Area of one stiffener
$n_s := 22$	Number of stiffeners within width b_0
$t := 16 \text{mm}$	Plate thickness
$L_s := 125 \text{m}$	Distance between supports

Calculations

$L_e := 0.7 \cdot L_s = 87500 \cdot \text{mm}$ Distance between adjacent points of zero bending

$A_{sl} := n_s \cdot A_s = 0.1303 \text{m}^2$

$$\alpha_0 := \sqrt{1 + \frac{A_{sl}}{b_0 \cdot t}} = 1.27$$

$$\kappa := \frac{\alpha_0 \cdot b_0}{L_e} = 0.20$$

$$\beta := \begin{cases} 1 & \text{if } \kappa < 0.02 \\ \frac{1}{1 + 6.4 \cdot \kappa^2} & \text{if } 0.02 < \kappa \leq 0.7 \end{cases} = 0.804$$

Effective^s width factor β for shear lag under elastic conditions. Relevant for serviceability and fatigue limit state

$$\beta_{ULS} := \beta^k = 0.958$$

Effective^s width factor β for shear lag under elastic-plastic conditions. Relevant for ultimate limit state

Input	
Bottom flange at sagging bending:	
$b_0 := 13712 \cdot \text{mm}$	Half width of flange
$A_{s_t} := 4997 \text{mm}^2$	Area of one trapezoidal stiffener
$A_{s_b} := 4127 \text{mm}^2$	Area of one bulb stiffener
$n_{s_t} := 10$	Number of trapezoidal stiffeners within width b_0
$n_{s_b} := 9.5$	Number of bulb stiffeners within width b_0
$t := 12 \text{mm}$	Plate thickness
$L_s := 125 \text{m}$	Distance between supports
Calculations	
$L_c := 0.7 \cdot L_s = 87500 \cdot \text{mm}$	Distance between adjacent points of zero bending
$A_{sl} := n_{s_t} \cdot A_{s_t} + n_{s_b} \cdot A_{s_b} = 0.0892 \text{m}^2$	
$\alpha_0 := \sqrt{1 + \frac{A_{sl}}{b_0 \cdot t}} = 1.24$	
$\kappa := \frac{\alpha_0 \cdot b_0}{L_c} = 0.19$	
$\beta := \begin{cases} 1 & \text{if } \kappa < 0.02 \\ \frac{1}{1 + 6.4 \cdot \kappa^2} & \text{if } 0.02 < \kappa \leq 0.7 \end{cases} = 0.805$	Effective ^s width factor β for shear lag under elastic conditions. Relevant for serviceability and fatigue limit state
$\beta_{ULS} := \beta^{\kappa} = 0.959$	Effective ^s width factor β for shear lag under elastic-plastic conditions. Relevant for ultimate limit state

Figure 6 shows the girder section at hogging bending. The flanges are supported by longitudinal girders, causing each flange to be separated into five widths where each width b_0 is half of the internal widths. Due to symmetry, some widths are identical. The calculations below give the β and β^{κ} factors for the top flange only.

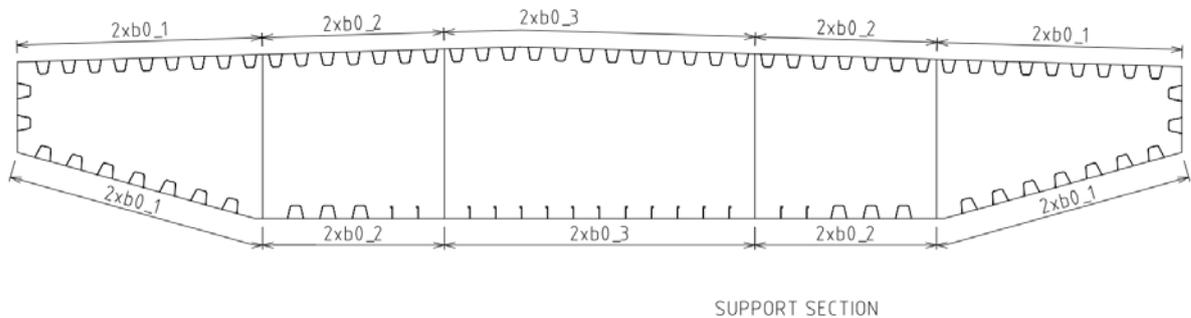


Figure 6 Section at hogging bending

NS-EN 1993-1-5 chapter 3.2 Effective^s width for shear lag and 3.3 Shear lag at the ultimate limit state

kNm := kN·m

Input

Top flange at hogging bending:

$b_{0,1} := 2844 \text{ mm}$	Half width of internal flange part 1
$b_{0,2} := 2095 \text{ mm}$	Half width of internal flange part 2
$b_{0,3} := 3595 \text{ mm}$	Half width of internal flange part 3
$A_s := 5923 \text{ mm}^2$	Area of one stiffener
$n_{s,1} := 4.5$	Number of stiffeners within width $b_{0,1}$
$n_{s,2} := 3.5$	Number of stiffeners within width $b_{0,2}$
$n_{s,3} := 6$	Number of stiffeners within width $b_{0,3}$
$t := 16 \text{ mm}$	Plate thickness
$L_s := 125 \text{ m}$	Distance between supports

Calculations

$L_c := 0.25(L_s + L_s) = 62500 \text{ mm}$ Distance between adjacent points of zero bending at

Internal flange part 1	Internal flange part 2	Internal flange part 3
$\Lambda_{sl,1} := n_{s,1} \cdot A_s = 0.0267 \text{ m}^2$	$\Lambda_{sl,2} := n_{s,2} \cdot A_s = 0.0207 \text{ m}^2$	$\Lambda_{sl,3} := n_{s,3} \cdot A_s = 0.0355 \text{ m}^2$
$\alpha_{0,1} := \sqrt{1 + \frac{\Lambda_{sl,1}}{b_{0,1} \cdot t}} = 1.26$	$\alpha_{0,2} := \sqrt{1 + \frac{\Lambda_{sl,2}}{b_{0,2} \cdot t}} = 1.27$	$\alpha_{0,3} := \sqrt{1 + \frac{\Lambda_{sl,3}}{b_{0,3} \cdot t}} = 1.27$
$\kappa_1 := \frac{\alpha_{0,1} \cdot b_{0,1}}{L_c} = 0.06$	$\kappa_2 := \frac{\alpha_{0,2} \cdot b_{0,2}}{L_c} = 0.04$	$\kappa_3 := \frac{\alpha_{0,3} \cdot b_{0,3}}{L_c} = 0.07$

$\beta_1 := \begin{cases} 1 & \text{if } \kappa_1 < 0.02 \\ \frac{1}{1 + 6.0 \left(\kappa_1 - \frac{1}{2500 \cdot \kappa_1} \right) + 1.6 \cdot \kappa_1^2} & \text{if } 0.02 < \kappa_1 \leq 0.7 \end{cases} = 0.765$ Effective^s width factor β for shear lag under elastic conditions. Relevant for serviceability and fatigue limit state

$\beta_{ULS,1} := \beta_1^{\kappa_1} = 0.985$ Effective^s width factor β for shear lag under elastic-plastic conditions. Relevant for ultimate limit state

$$\beta_2 := \begin{cases} 1 & \text{if } \kappa_2 < 0.02 \\ \frac{1}{1 + 6.0 \left(\kappa_2 - \frac{1}{2500 \cdot \kappa_2} \right) + 1.6 \cdot \kappa_2^2} & \text{if } 0.02 < \kappa_2 \leq 0.7 \end{cases} = 0.832$$

Effective^s width factor β for shear lag under elastic conditions. Relevant for serviceability and fatigue limit state

$$\beta_{ULS\ 2} := \beta_2^{\kappa_2} = 0.992$$

Effective^s width factor β for shear lag under elastic-plastic conditions. Relevant for ultimate limit state

$$\beta_3 := \begin{cases} 1 & \text{if } \kappa_3 < 0.02 \\ \frac{1}{1 + 6.0 \left(\kappa_3 - \frac{1}{2500 \cdot \kappa_3} \right) + 1.6 \cdot \kappa_3^2} & \text{if } 0.02 < \kappa_3 \leq 0.7 \end{cases} = 0.707$$

Effective^s width factor β for shear lag under elastic conditions. Relevant for serviceability and fatigue limit state

$$\beta_{ULS\ 3} := \beta_3^{\kappa_3} = 0.975$$

Effective^s width factor β for shear lag under elastic-plastic conditions. Relevant for ultimate limit state

3.2 Summary of shear lag factors for all cross-sections

CONCEPT K12								Elastic (SLS, FLS)		Elastic-plastic (ULS)		
Span	125m	b ₀ top	b ₀ bot	Le	κ top	κ bot	a ₀ top	a ₀ bot	β top	β bot	β top	β bot
Cross-section	[m]	[m]	[m]	[m]	[-]	[-]	[-]	[-]	[-]	[-]	[-]	[-]
Field (F1_rev05)	13,51	13,71	87,50	0,20	0,19	1,27	1,24	0,80	0,80	0,96	0,96	
Field (F2_rev00)	13,51	13,71	87,50	0,20	0,19	1,27	1,21	0,80	0,81	0,96	0,96	
Transition (T1_rev00) – sagging bending												
Section b0_1	4,95	5,05	87,50	0,07	0,07	1,27	1,21	0,97	0,97	1,00	1,00	
Section b0_2	3,60	3,60	87,50	0,05	0,05	1,27	1,23	0,98	0,98	1,00	1,00	
Section b0_3	4,95	5,05	87,50	0,07	0,07	1,27	1,21	0,97	0,97	1,00	1,00	
Transition (T1_rev00) – hogging bending												
Section b0_1	4,95	5,05	62,50	0,10	0,10	1,27	1,21	0,63	0,63	0,95	0,96	
Section b0_2	3,60	3,60	62,50	0,07	0,07	1,27	1,23	0,71	0,71	0,97	0,98	
Section b0_3	4,95	5,05	62,50	0,10	0,10	1,27	1,21	0,63	0,63	0,95	0,96	
Transition (T1_rev00) – Linear interpolation between sagging bending and hogging bending												
Section b0_1	4,95	5,05						0,80	0,80	0,98	0,98	
Section b0_2	3,60	3,60						0,84	0,85	0,99	0,99	
Section b0_3	4,95	5,05						0,80	0,80	0,98	0,98	
Support (S1_rev02)												
Section b0_1	2,84	2,95	62,50	0,06	0,06	1,27	1,18	0,77	0,77	0,99	0,99	
Section b0_2	2,10	2,10	62,50	0,04	0,04	1,27	1,17	0,83	0,85	0,99	0,99	
Section b0_3	3,59	3,60	62,50	0,07	0,07	1,27	1,19	0,71	0,73	0,98	0,98	
Section b0_4	2,10	2,10	62,50	0,04	0,04	1,27	1,17	0,83	0,85	0,99	0,99	
Section b0_5	2,84	2,95	62,50	0,06	0,06	1,27	1,18	0,77	0,77	0,98	0,99	
Support (S2_rev00)												

Section b0_1	2,84	2,95	62,50	0,06	0,06	1,27	1,19	0,76	0,77	0,98	0,99
Section b0_2	2,10	2,10	62,50	0,04	0,04	1,27	1,17	0,83	0,85	0,99	0,99
Section b0_3	3,59	3,60	62,50	0,07	0,07	1,27	1,17	0,71	0,73	0,97	0,98
Section b0_4	2,10	2,10	62,50	0,04	0,04	1,27	1,17	0,83	0,85	0,99	0,99
Section b0_5	2,84	2,95	62,50	0,06	0,06	1,27	1,19	0,76	0,77	0,98	0,99

4 Plate buckling effects

The bridge girder is a member in cross-section class 4, meaning local buckling will occur before the attainment of yield stress in one or more parts of the cross-section.

Sufficient capacity of the bridge girder subject to compression and biaxial bending is verified based on equation (4.15) in NS-EN 1993-1-5:2006 + NA 2009. Equation (4.15) is a linear summation of the utilization that each force component utilizes the capacity corresponding to the respective type of force. Due to the bridge girders geometric shape with an inclined bottom plate, the summation of the utilization will give conservative utilization results for biaxial bending when the utilization about each axis is large at the same time, see Figure 7.

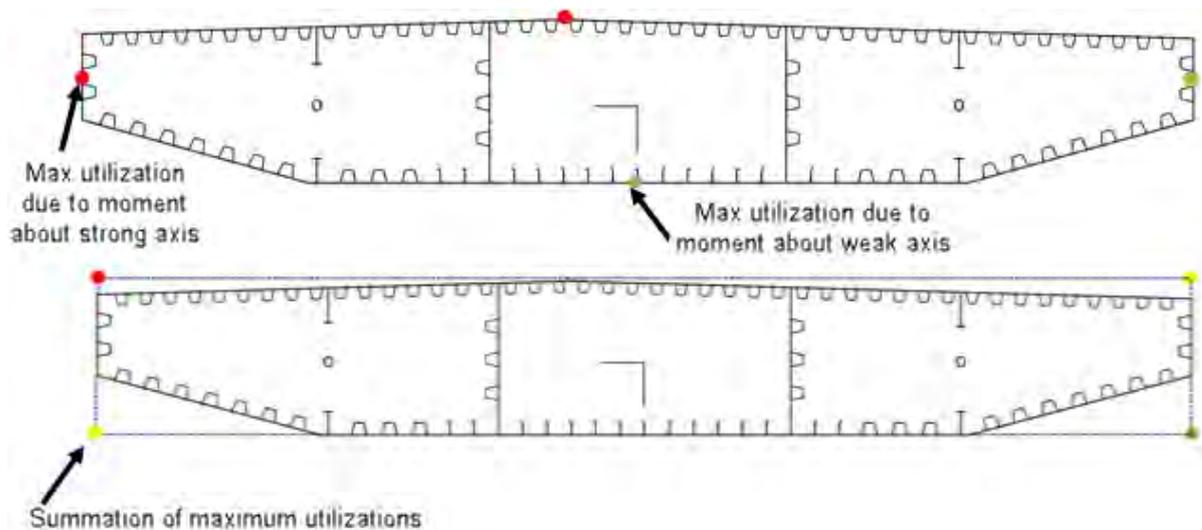


Figure 7 Illustration of the capacity check combining maximum utilizations of the moment about each axis

Since the Eurocode does not account for conservative utilizations due to geometric shapes, a second way of performing the capacity check has been introduced. This second method is denoted method 2 in the results given in a closure to 90-RE-107 Appendix G: Global Analyses – Response_0, while the method described above is denoted method 1.

For method 2, the utilization at all the 7 extremity points of the girder is calculated based on the effective elastic section modulus for the specific point.

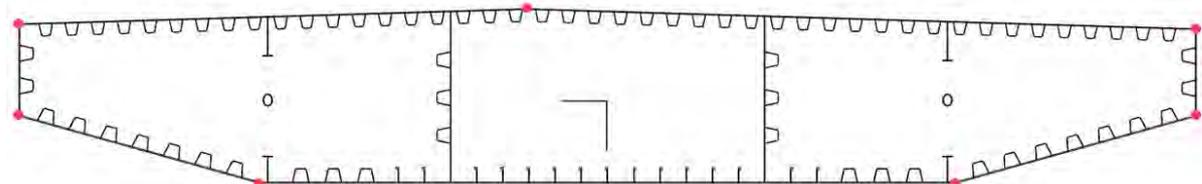


Figure 8 The 7 extremity points of the bridge girder controlled with method 2 of the capacity check

As shown in section 5 of this memo, the effective^p cross-sectional area of the girder in compression is always larger than 0.5 times the gross cross-sectional area, hence plate buckling effects on the stiffness is ignored in the global analysis in accordance with clause 2.2(5) in EC3-5.

4.1 Break-down of equation 4.15 of EC3-5

A modified version of equation (4.15) is shown below. The equation is modified to adapt to the axis notation and force direction of this project.

$$\eta_1 = -\frac{N_{Ed}}{f_y A_{eff}} + \frac{M_{weak,Ed} + N_{Ed} e_{w,N}}{f_y W_{weak,eff}} + \frac{M_{strong,Ed} + N_{Ed} e_{s,N}}{f_y W_{strong,eff}} \quad \text{modified (4.15)}$$

Where

A_{eff} is

- $A_{eff,c}$ – effective^p cross-section area when N_{Ed} is axial compression
- $A_{eff,t}$ – gross cross-section area when N_{Ed} is axial tension

$e_{w,N}$ and $e_{s,N}$ is

- $e_{w,N,c}$ - eccentricity of the neutral axis in vertical direction when N_{Ed} is axial compression. Gives an additional moment about the weak axis.
- $e_{w,N,t}$ - zero when N_{Ed} is axial tension. No eccentricity moment
- $e_{s,N,c}$ - eccentricity of the neutral axis in horizontal direction when N_{Ed} is axial compression. Gives an additional moment about the strong axis.
- $e_{s,N,t}$ - zero when N_{Ed} is axial tension. No eccentricity moment

For method 1 of the capacity check, the equation is applied one time for the entire girder. Where

$W_{weak,eff}$ is

- $W_{weak,eff}^+$ – effective elastic section modulus for a positive moment about the weak axis
- $W_{weak,eff}^-$ – effective elastic section modulus for a negative moment about the weak axis

$W_{strong,eff}$ is

- $W_{strong,eff}^+$ – effective^p elastic section modulus for a positive moment about the strong axis
- $W_{strong,eff}^-$ – effective^p elastic section modulus for a negative moment about the strong axis

For method 2 of the capacity check, the equation is applied for the 7 extremity points of the girder.

Where

$W_{weak,eff}$ is

- $W_{weak,eff}^+$ – effective elastic section modulus for each specific point on the girder for a positive moment about the weak axis
- $W_{weak,eff}^-$ – effective elastic section modulus for each specific point on the girder for a negative moment about the weak axis

$W_{strong,eff}$ is

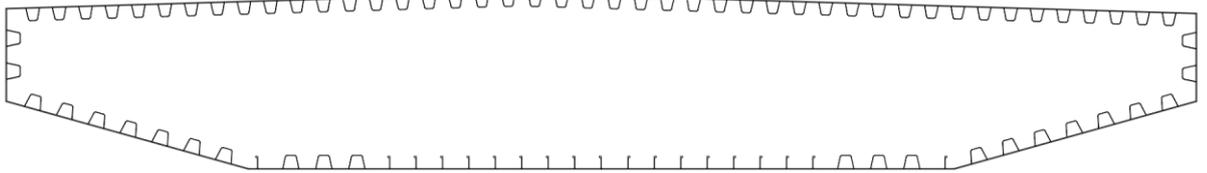
- $W_{strong,eff}^+$ – effective^p elastic section modulus for each specific point on the girder for a positive moment about the strong axis

- $W_{strong,eff}$ – effective^p elastic section modulus for each specific point on the girder for a negative moment about the strong axis

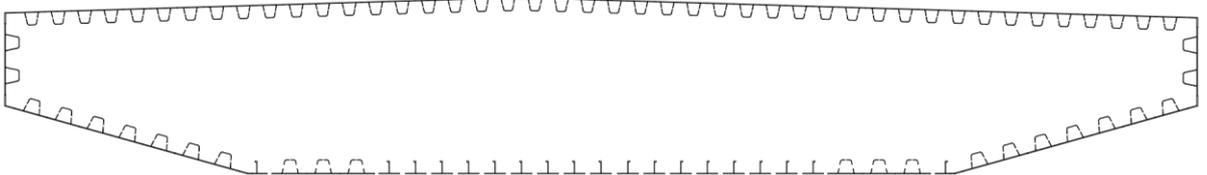
4.2 Effective cross-sections

As explained above, verification with equation (4.15) requires cross-sectional data for six different effective cross-sections depending on the direction of N_{Ed} , $M_{weak,Ed}$ and $M_{strong,Ed}$:

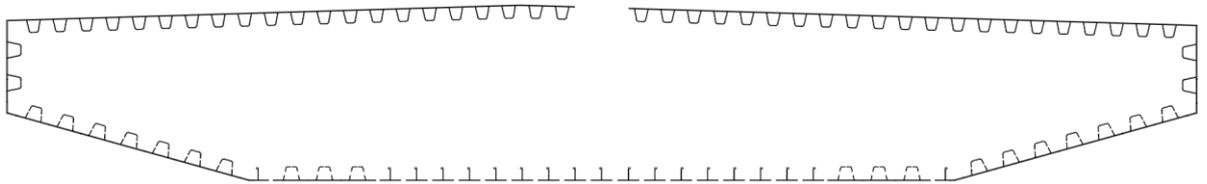
1. Gross cross-section for N_{Ed} as a tensional force, ie. the whole cross-section is in the tension zone and there are no bucklings effects due to this force component



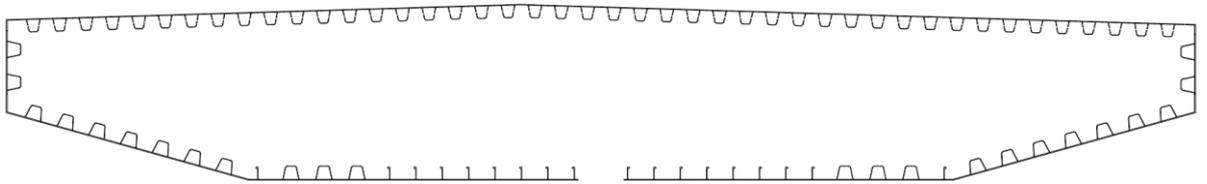
2. Effective^p cross-section for N_{Ed} as a compressional force, ie. the whole cross-section is in the compression zone.



3. Effective cross-section for $M_{weak,Ed}$ as a positive moment about the horizontal axis, ie. all parts below the horizontal neutral axis is in the compression zone. Shear lag effects of the compression and tension flange are included.

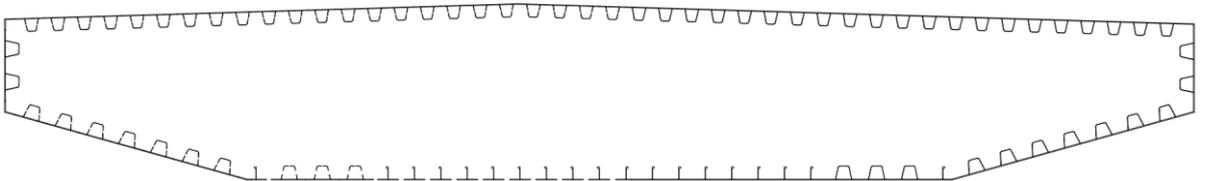


4. Effective cross-section for $M_{weak,Ed}$ as a negative moment about the horizontal axis, ie. all parts above the horizontal neutral axis is in the compression zone. Shear lag effects of the compression and tension flange are included.



5. Effective^p cross-section for $M_{strong,Ed}$ as a positive moment about the vertical axis, ie. all parts east of the vertical neutral axis is in the compression zone.

6. Effective^p cross-section for $M_{strong,Ed}$ as a negative moment about the vertical axis, ie. all parts west of the vertical neutral axis is in the compression zone.



Due to symmetry, the effective^p cross-sections for $M_{strong,Ed}$ as a positive moment is the mirrored of the effective^p cross-sections for $M_{strong,Ed}$ as a negative moment.

The effective^p area of the compression zone in each of the effective^p cross-sections is the effective^p area of each stiffener and the effective^p part of the panel between the stiffeners. Both local buckling of each plate element and global buckling of the stiffened panel is accounted for.

The reduction factors, ρ_{loc} and ρ_c , due to plate buckling is calculated as explained in the following sections.

4.2.1 Local plate buckling effects

The reduction factor ρ_{loc} for all subpanels in cross-section class 4 in the compression zone is calculated according to clause 4.4(2) of EC3-5. The stress distribution within all internal compression elements are conservatively set to constant. This gives a buckling factor k_σ of 4.0 for all elements, and the effective width of the internal element is distributed with half of the effective width to each side of the element, see Figure 9.

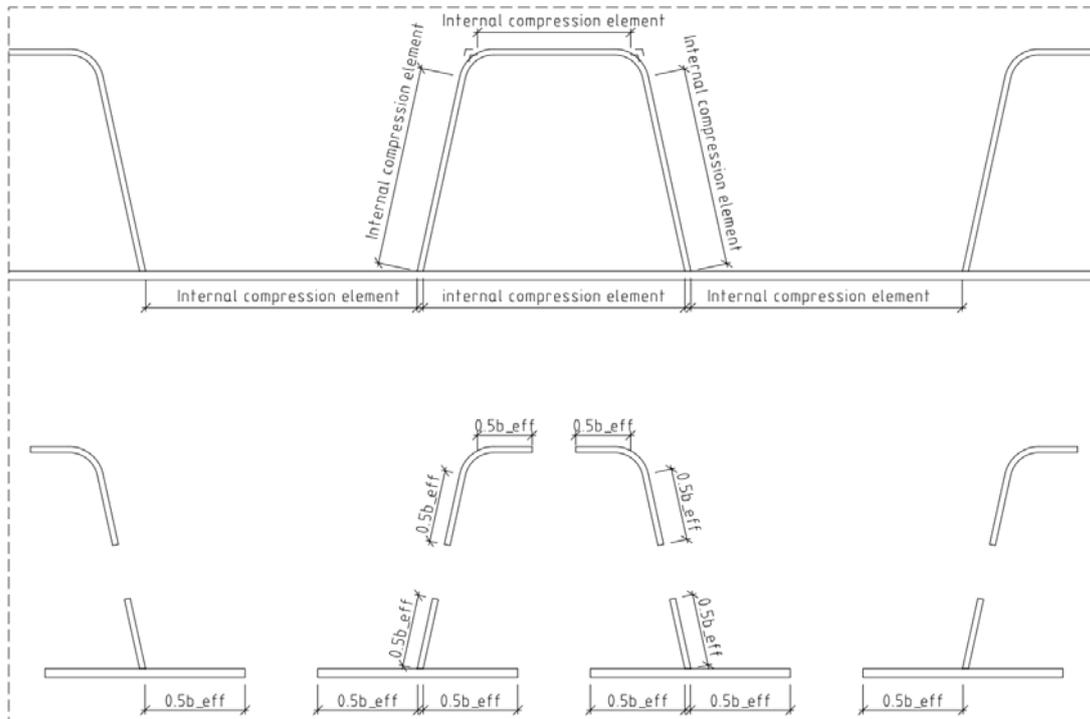


Figure 9 Illustration of effective^p widths due to local buckling of internal compression elements

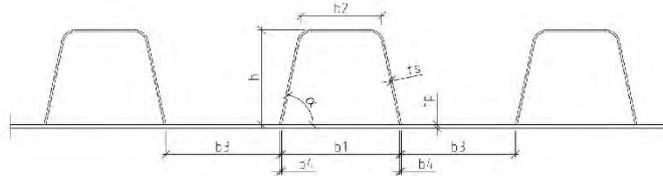
Calculation example of local buckling effects

NS-EN 1993-1-5 chapter 4 Plate buckling effects due to direct stresses at the ultimate limit state and 3.3 Shear lag at the ultimate limit state

kNm := kN·m

Input

Concept K12, Stiffener ID K12-F1-T



- $E_{mod} := 210000\text{MPa}$ modulus of elasticity
- $\psi := 1.0$ stress ratio (constant)
- $f_{yp} := 420\text{MPa}$ yield strength skin plate
- $f_{ys} := 420\text{MPa}$ yield strength stiffener
- $a := 4000\text{mm}$ plate length (distance between transverse stiffeners)
- $c_{c_stiffener} := 600\text{mm}$ center distance between stiffeners
- $b_1 := 300\text{mm}$ internal width of skin plate in stiffener
- $b_2 := 185\text{mm}$ width of stiffener flange
- $h := 286\text{mm}$ stiffener height
- $t_p := 14\text{mm}$ thickness skin plate
- $t_s := 8\text{mm}$ thickness stiffener
- $\alpha_s := 0.34$ imperfection factor for stiffener (closed = 0.34, open = 0.49)
- $\beta_{ULS} := 0.955$ shear lag factor at ULS

Calculations

$\epsilon_s := \sqrt{\frac{235\text{MPa}}{f_{ys}}} = 0.75$	correction factor for yield strength stiffener
$\epsilon_p := \sqrt{\frac{235\text{MPa}}{f_{yp}}} = 0.75$	correction factor for yield strength skin plate
$b_s := \sqrt{\left(h - \frac{t_s}{2}\right)^2 + \left[\frac{t_s}{2} + 0.5 \cdot (b_1 - b_2)\right]^2} = 289\text{ mm}$	length of inclined stiffener web
$\alpha := \text{asin}\left[\frac{(h - 0.5t_s)}{b_s}\right] = 77.70\text{ deg}$	
$b_4 := \frac{t_s}{\sin(\alpha)} = 8.19\text{ mm}$	width of skin plate by stiffener
$b_3 := c_c_stiffener - b_1 - 2b_4 = 283.62\text{ mm}$	width of skin plate between stiffeners
Gross cross section properties	
$A_{st} := t_s \cdot (2 \cdot b_s + b_2) = 6098\text{ mm}^2$	area of stiffener
$A_p := t_p \cdot c_c_stiffener = 8400\text{ mm}^2$	area of skin plate
$A_{sl\ 1} := A_{st} + A_p = 14498\text{ mm}^2$	area of stiffened plate
$y_{cl} := \frac{b_2 \cdot t_s \cdot \left(t_p + h - \frac{t_s}{2}\right) + 2 \cdot b_s \cdot t_s \cdot \left(t_p + \frac{h - t_s}{2}\right) + A_p \cdot \frac{t_p}{2}}{A_{sl\ 1}} = 83.01\text{ mm}$	CoG of stiffened plate from below skin plate
$I_{sl\ 1} := 2 \cdot \frac{1}{12} \cdot h^3 \cdot \frac{t_s}{\sin(\alpha)} + 2 \cdot b_s \cdot t_s \cdot \left(\frac{h - t_s}{2} + t_p - y_{cl}\right)^2 + b_2 \cdot t_s \cdot \left(t_p + h - \frac{t_s}{2} - y_{cl}\right)^2 + A_p \cdot \left(y_{cl} - \frac{t_p}{2}\right)^2$... = 170217649·mm ⁴	second moment of area for stiffened plate
$i := \sqrt{\frac{I_{sl\ 1}}{A_{sl\ 1}}} = 108\text{ mm}$	radius of gyration of stiffened plate
$y_{st} := \frac{b_2 \cdot t_s \cdot \left(h - \frac{t_s}{2}\right) + 2 \cdot b_s \cdot t_s \cdot \left(\frac{h - t_s}{2}\right)}{A_{st}} = 174\text{ mm}$	CoG of stiffener from above skin plate
$e_1 := y_{st} + t_p - y_{cl} = 105\text{ mm}$	distance between CoG of stiffened plate and CoG of stiffener
$e_2 := y_{cl} - \frac{t_p}{2} = 76\text{ mm}$	distance between CoG of stiffened plate and CoG of skin plate

Local buckling of internal plate elements according to NS-EN 1993-1-5 4.5.1(4)

Internal width of skin plate in stiffener, b_1

$$\text{class}_{b1} := \begin{cases} \text{"1-3"} & \text{if } \frac{b_1}{t_p} \leq 42 \cdot \epsilon_p = \text{"1-3"} \\ \text{"4"} & \text{otherwise} \end{cases} \quad \text{class}$$

$$k_{\sigma b1} := \begin{cases} \text{"no local buckling"} & \text{if } \text{class}_{b1} = \text{"1-3"} = \text{"no local buckling"} \\ 4 & \text{otherwise} \end{cases} \quad \text{buckling factor}$$

$$\lambda_{b1} := \begin{cases} \text{"no local buckling"} & \text{if } k_{\sigma b1} = \text{"no local buckling"} = \text{"no local buckling"} \\ \frac{\frac{b_1}{t_p}}{28.4 \cdot \epsilon_p \cdot \sqrt{k_{\sigma b1}}} & \text{otherwise} \end{cases} \quad \text{slenderness}$$

$$\rho_{b1} := \begin{cases} 1 & \text{if } (\lambda_{b1} = \text{"no local buckling"}) \vee \lambda_{b1} \leq 0.5 + \sqrt{0.085 - 0.055 \cdot \psi} = 1.000 \\ \min \left[1, \frac{\lambda_{b1} - 0.055 \cdot (3 + \psi)}{\lambda_{b1}^2} \right] & \text{otherwise} \end{cases} \quad \text{reduction factor}$$

$$b_{eff, b1} := b_1 \cdot \rho_{b1} = 300\text{-mm} \quad \text{effective width}$$

Stiffener flange, b_2

$$\text{class}_{b2} := \begin{cases} \text{"1-3"} & \text{if } \frac{b_2}{t_s} \leq 42 \cdot \epsilon_s = \text{"1-3"} \\ \text{"4"} & \text{otherwise} \end{cases} \quad \text{class}$$

$$k_{\sigma b2} := \begin{cases} \text{"no local buckling"} & \text{if } \text{class}_{b2} = \text{"1-3"} = \text{"no local buckling"} \\ 4 & \text{otherwise} \end{cases} \quad \text{buckling factor}$$

$$\lambda_{b2} := \begin{cases} \text{"no local buckling"} & \text{if } k_{\sigma b2} = \text{"no local buckling"} = \text{"no local buckling"} \\ \frac{\frac{b_2}{t_s}}{28.4 \cdot \epsilon_s \cdot \sqrt{k_{\sigma b2}}} & \text{otherwise} \end{cases} \quad \text{slenderness}$$

$$\rho_{b2} := \begin{cases} 1 & \text{if } (\lambda_{b2} = \text{"no local buckling"}) \vee \lambda_{b2} \leq 0.5 + \sqrt{0.085 - 0.055 \cdot \psi} = 1.000 \\ \min \left[1, \frac{\lambda_{b2} - 0.055 \cdot (3 + \psi)}{\lambda_{b2}^2} \right] & \text{otherwise} \end{cases} \quad \text{reduction factor}$$

$$b_{eff, b2} := b_2 \cdot \rho_{b2} = 185\text{-mm} \quad \text{effective width}$$

Width of skin plate between stiffeners, b_3

$$\text{class}_{b_3} := \begin{cases} \text{"1-3"} & \text{if } \frac{b_3}{t_p} \leq 42 \cdot \epsilon_p = \text{"1-3"} \\ \text{"4"} & \text{otherwise} \end{cases} \quad \text{class}$$

$$k_{\sigma b_3} := \begin{cases} \text{"no local buckling"} & \text{if } \text{class}_{b_3} = \text{"1-3"} = \text{"no local buckling"} \\ 4 & \text{otherwise} \end{cases} \quad \text{buckling factor}$$

$$\lambda_{b_3} := \begin{cases} \text{"no local buckling"} & \text{if } k_{\sigma b_3} = \text{"no local buckling"} = \text{"no local buckling"} \\ \frac{\frac{b_3}{t_p}}{28.4 \cdot \epsilon_p \cdot \sqrt{k_{\sigma b_3}}} & \text{otherwise} \end{cases} \quad \text{slenderness}$$

$$\rho_{b_3} := \begin{cases} 1 & \text{if } (\lambda_{b_3} = \text{"no local buckling"}) \vee \lambda_{b_3} \leq 0.5 + \sqrt{0.085 - 0.055 \cdot \psi} = 1.000 \\ \min \left[1, \frac{\lambda_{b_3} - 0.055 \cdot (3 + \psi)}{\lambda_{b_3}^2} \right] & \text{otherwise} \end{cases} \quad \text{reduction factor}$$

$$b_{\text{eff}_b} := b_3 \cdot \rho_{b_3} = 284 \cdot \text{mm} \quad \text{effective width}$$

Inclined stiffener web, b_s

$$\text{class}_{b_s} := \begin{cases} \text{"1-3"} & \text{if } \frac{b_s}{t_s} \leq 42 \cdot \epsilon_s = \text{"4"} \\ \text{"4"} & \text{otherwise} \end{cases} \quad \text{class}$$

$$k_{\sigma b_s} := \begin{cases} \text{"no local buckling"} & \text{if } \text{class}_{b_s} = \text{"1-3"} = 4 \\ 4 & \text{otherwise} \end{cases} \quad \text{buckling factor}$$

$$\lambda_{b_s} := \begin{cases} \text{"no local buckling"} & \text{if } k_{\sigma b_s} = \text{"no local buckling"} = 0.85 \\ \frac{\frac{b_s}{t_s}}{28.4 \cdot \epsilon_s \cdot \sqrt{k_{\sigma b_s}}} & \text{otherwise} \end{cases} \quad \text{slenderness}$$

$$\rho_{b_s} := \begin{cases} 1 & \text{if } (\lambda_{b_s} = \text{"no local buckling"}) \vee \lambda_{b_s} \leq 0.5 + \sqrt{0.085 - 0.055 \cdot \psi} = 0.873 \\ \min \left[1, \frac{\lambda_{b_s} - 0.055 \cdot (3 + \psi)}{\lambda_{b_s}^2} \right] & \text{otherwise} \end{cases} \quad \text{reduction factor}$$

$$b_{\text{eff}_{b_s}} := b_s \cdot \rho_{b_s} = 252 \cdot \text{mm} \quad \text{effective width}$$

Effective^p_{loc} area after reduction due to local plate buckling

$$A_{\text{st_eff_loc}} := t_s \cdot (2 \cdot b_{\text{eff}_{b_s}} + b_{\text{eff}_{b_2}}) = 5509 \text{ mm}^2 \quad \text{effective^p_{loc} area of stiffener}$$

$$A_{\text{p_eff_loc}} := t_p \cdot (2 \cdot b_4 + b_{\text{eff}_{b_1}} + b_{\text{eff}_{b_3}}) = 8400 \text{ mm}^2 \quad \text{effective^p_{loc} area of skin plate}$$

$$A_{\text{sl_1_eff_loc}} := A_{\text{st_eff_loc}} + A_{\text{p_eff_loc}} = 13909 \text{ mm}^2 \quad \text{effective^p_{loc} area of stiffened plate}$$

4.2.2 Global plate buckling effects

Plate type behavior

Since all plates of the bridge girder are heavily stiffened, the plate type buckling behavior is ignored because the column type behavior will prevail.

Column type buckling behavior

The global reduction factor ρ_c due to column type buckling behavior of a stiffener and the adjacent part of panel between the stiffeners is calculated in accordance with section 4.5.3 of EC3-5.

Clause 4.5.3(3) states that the elastic critical column buckling stress $\sigma_{cr,c}$ may be determined from the elastic critical column buckling stress $\sigma_{cr,sl}$ of the stiffener closest to the panel edge with the highest compressive stress.

Due to different types of stiffeners, trapezoidal and bulbs, in the bottom plate, the reduction factor ρ_c is calculated separately for each type of stiffener based on their respective elastic critical column buckling stress $\sigma_{cr,sl}$.

Example calculation of global buckling effects (continuation of example for local buckling effects)

Global column type buckling according to NS-EN 1993-1-5 4.5.3

$\beta_{Ac} := \frac{A_{sl,1,eff,loc}}{A_{sl,1}} = 0.96$	correction factor for column slenderness
$\sigma_{cr,e} := \frac{\pi^2 \cdot E_{mod} \cdot I_{sl,1}}{A_{sl,1} \cdot d^2} = 1521 \cdot \text{MPa}$	elastic critical column buckling stress
$\lambda_c := \sqrt{\frac{\beta_{Ac} \cdot f_{ys}}{\sigma_{cr,e}}} = 0.51$	relative column slenderness
$\alpha_{s,e} := \alpha_s + \frac{0.09}{\max(e_1, e_2)} = 0.43$	modified imperfection factor NS-EN 1993-1-5 eq. 4.12
$\Phi_c := 0.5 \cdot \left[1 + \alpha_{s,e} \cdot (\lambda_c - 0.2) + \lambda_c^2 \right] = 0.70$	function used to calculate column type buckling reduction factor
$\rho_c := \frac{1}{\Phi_c + \sqrt{\Phi_c^2 - \lambda_c^2}} = 0.852$	global reduction factor due to column type buckling

4.2.3 Combined local and global plate buckling effects

In accordance with clause 4.5.1(3), the final effective^p area of the compression zone in the bridge girder is the effective^p area reduced due to local buckling times the reduction factor due to global buckling, except the effective^p parts of skin plate which is supported by an adjacent plate, which is not to be reduced due to global buckling effects:

$$A_{c,eff} = \rho_c A_{c,eff,loc} + \Sigma b_{edge,eff} t$$

As mentioned, the global reduction factor ρ_c will differ depending on the type of stiffener, hence the equation above may be rewritten as

$$A_{c,eff} = \Sigma \rho_{c,sl} A_{sl,eff,loc} + \Sigma b_{edge,eff} t$$

Where $A_{sl,eff,loc}$ is the effective^p area of a stiffener and the adjacent part of panel reduced for local buckling, and $\rho_{c,sl}$ is the global reduction factor corresponding to the same type of stiffener.

When calculating the geometric properties A_{eff} and W_{eff} for the effective^p girder composed of different plates, the global reduction factor $\rho_{c,sl}$ is taken into account by reducing the thickness of the skin plate and the thickness of the stiffeners.

Effective^p area after reduction due to local and global buckling

$A_{st_eff_p} := \rho_c \cdot A_{st_eff_loc} = 4695 \text{ mm}^2$	effective ^p area of stiffener
$A_{p_eff_p} := \rho_c \cdot A_{p_eff_loc} = 7158 \text{ mm}^2$	effective ^p area of skin plate
$A_{st_l_eff_p} := \rho_c \cdot A_{st_l_eff_loc} = 11852 \text{ mm}^2$	effective ^p area of stiffened plate

4.2.4 Combined shear lag and plate buckling effects

The elastic-plastic shear lag effects are combined with the effects of plate buckling due to direct stresses at the ultimate limit state according to equation (3.5) of EC3-5:

$$A_{eff} = A_{c,eff} \beta^k$$

Where $A_{c,eff}$ is the effective^p area of the compression flange. For the tension flange, the effective width $b_{eff} = b_0 \beta^k$ is adapted.

When calculating the geometric property W_{eff} for the effective girder, the shear lag reduction factor β^k is taken into account by reducing the thickness of the skin plate and the thickness of the stiffeners in the compression flange.

Combined shear lag and buckling effects

Effective area after reduction due to shear lag and buckling effects

$A_{st_eff} := \beta_{ULS} \cdot A_{st_eff_p} = 4483 \text{ mm}^2$	effective area of stiffener
$A_{p_eff} := \beta_{ULS} \cdot A_{p_eff_p} = 6836 \text{ mm}^2$	effective area of skin plate
$A_{st_l_eff} := \beta_{ULS} \cdot A_{st_l_eff_p} = 11319 \text{ mm}^2$	effective area of stiffened plate

5 Cross-section data

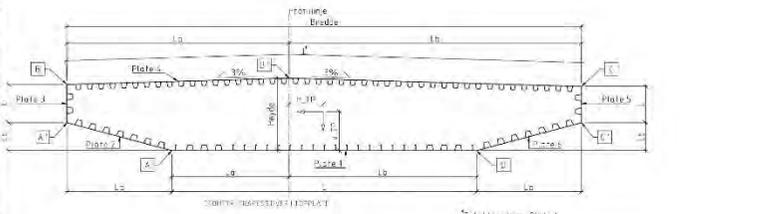
On the following pages, cross-sectional data of the typical bridge girder sections at mid span and by columns are given:

Shear lag and buckling effects of Bridge Girders

Concept development, Floating bridge E39 Bjørnafjordn

K12_F3

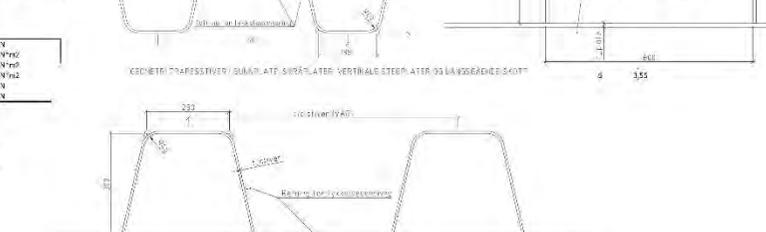
Section	K12_F1_rev05 K12_F1_05	Transverse section - normal - concept E12	Revision status Last: 14/05/2019 by: []	EDM Total bredde Total høyde	07.06.2019 @ 13:30	
Bredde	27 [m]			27.021		
Høyde	4 [m]			4.012		
Flisestørrelse [mm]	Plate 1	Plate 2	Plate 3	Plate 4	Plate 5	Plate 6
t [mm]	6,336	5,509	121	11,644	5,509	12
b [mm]	9,802	15,350		15,350	1,540	
h [mm]	16,000	5,511	2,511	2,511	2,000	5,511
Flisestørrelse type	K12_F1-0	K12_F2-0	K12_F1-0	K12_F1-0	K12_F1-0	K12_F1-0
Transversal thickness [mm]	6	6	6	6	6	6
Transversal type [mm]	0,256	0,486	0,75	0,900	0,75	0,256
Stål type	K12_1 H 1					
Width h [mm]	280					
Transverse [mm]	51					
Butt fastset [mm]	15					
Butt fastset c [mm]	40					
Butt width [mm]	62					
Butt c/c [mm]	0,5					



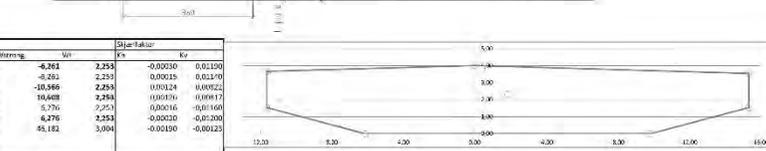
Tyngdepunkt					
HTP (Fra Pjott) [m]	-2,834				
YHP (Fra L1) [m]	2,541				
HTP (Fra L1) [m]	0,336				
YHP (Fra L1) [m]	2,222				

Effekt	7,85	27m/s
Formid	2,50E+05	kgm
Polynom	0,3	
Conduct	8,00E+04	kgm

Brukshorisont		0,074 m2
Formål: Brukshorisont		
Areall	2,270 m2	
Ungedehent, No L1C	1,167 m2	
Ungedehent, No L1C	2,200 m2	
Formål: Brukshorisont	8,111 m2	
Sjæneral vertikalt*	0,0281 m2	
Sjæneral horisontal*	0,0000 m2	
2. Areallområde, stakk aksel**	2,559 m2	
2. Areallområde, stakk aksel***	2,271 m2	
2. Areallområde, stakk aksel****	2,559 m2	
2. Areallområde, stakk aksel*****	0,4598 m2	
Ungedehent**	731,547 m2/m	
Masse areal	0,977 m	
Masse vertikalt	2,000 m	
Surf areal	11,227 m	
Masse rekkverk	0,721 m	
Masse dekk	4,622 m	
Surf masse	12,429 m	
Formål: Brukshorisont	1,200 m	
Masse brukshorisont	10,000 m	



Bøyemoment	Bøyemoment		Bøyemoment		Bøyemoment		Bøyemoment		Bøyemoment	
	mm	mm	mm	mm	mm	mm	mm	mm	mm	mm
Punkt C, topp øst	-15,362	3,551	0,012	-2,106	2,864	2,810	-6,261	2,256	-0,0010	0,01190
Punkt C, bunn øst	-15,362	3,551	0,012	-2,106	2,864	2,810	-6,261	2,256	-0,0010	0,01190
Punkt D, bunn øst	-9,850	0,000	0,012	-1,102	-1,478	-10,566	2,256	0,00124	0,00222	
Punkt A, bunn vest	6,168	0,000	0,012	-1,102	-1,478	10,668	2,256	0,00170	0,00117	
Punkt A, topp vest	11,665	1,554	0,012	-1,256	-4,198	4,376	2,253	0,00016	-0,01160	
Punkt B, topp vest	31,462	3,662	0,012	1,910	2,443	6,276	2,253	-0,00210	-0,01200	
Punkt B'	0,000	0,012	-0,015	1,528	1,937	2,045	45,182	3,094	-0,00100	-0,00125



Metode 1	Effektive bøyemomentdata for påvisning av brukshorisontens kapasitet mot trykk og toakslert bøyning	Metode 2	Effektive bøyemomentdata for påvisning av brukshorisontens kapasitet mot trykk og toakslert bøyning
Aeff,C	5,004 m2	Aeff,C	1,004 m2
Aeff,T	2,270 m2	Aeff,T	2,270 m2
Aw,N,C	-0,064 m	Aw,N,C	0,000 m
Aw,N,T	0,01 m	Aw,N,T	0,000 m
Aw,N,C	0,01 m	Aw,N,C	0,000 m
Aw,N,T	0,01 m	Aw,N,T	0,000 m
W'weak,off	1,07 m3	W'weak,off	1,07 m3
W'weak,off	-0,01 m3	W'weak,off	-0,01 m3
W'strong,off	5,300 m3	W'strong,off	5,300 m3
W'strong,off	5,300 m3	W'strong,off	5,300 m3



Metode 2	Effektive bøyemomentdata for påvisning av brukshorisontens kapasitet mot trykk og toakslert bøyning	Metode 2	Effektive bøyemomentdata for påvisning av brukshorisontens kapasitet mot trykk og toakslert bøyning
Aeff,C	1,004 m2	Aeff,C	1,004 m2
Aeff,T	2,270 m2	Aeff,T	2,270 m2
Aw,N,C	0,064 m	Aw,N,C	0,000 m
Aw,N,T	0,000 m	Aw,N,T	0,000 m
Aw,N,C	0,000 m	Aw,N,C	0,000 m
Aw,N,T	0,000 m	Aw,N,T	0,000 m
W'weak,off	-2,693	W'weak,off	-2,693
W'weak,off	-2,16	W'weak,off	-2,16
Punkt C, topp øst	-2,693	W'weak,off	-2,693
Punkt C'	-2,16	W'weak,off	-2,16
Punkt D, bunn øst	1,078	W'weak,off	1,078
Punkt A, bunn vest	1,078	W'weak,off	1,078
Punkt A'	2,081	W'weak,off	2,081
Punkt B, topp vest	-2,437	W'weak,off	-2,437
Punkt B'	-1,823	W'weak,off	-1,823



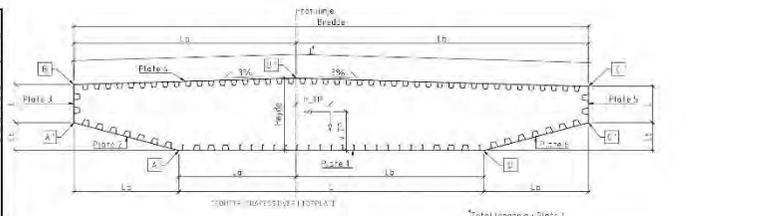
Reduksjonsfaktorer	Plate 1	Plate 2	Plate 3	Plate 4	Plate 5	Plate 6
Trapesoidstiffness and adjacent part of skin plate						
σ handling	0,743	0,777	0,743	0,806	0,743	0,777
σ handling 2-nd shear lag ULS	0,714	0,743	0,714	0,769	0,714	0,743
σ handling	0,687					
σ handling 2-nd shear lag ULS	0,653					

Shear lag and buckling effects of Bridge Girders

Concept development, Floating bridge E39 Bjørnafjorden

K12_F2

Section	K12_F2_000 K12_F2_00	Truss section - normal - concept K12	Section data Last: 145 kN/m	EDM Total breadth Total height		
Breadth	27 [m]			27.025		
Height	4 [m]			4.01		
Truss section	Plate 1	Plate 2	Plate 3	Plate 4	Plate 5	Plate 6
Truss height [mm]	14	14	14	14	14	14
e [m]	0.300	0.300	0.300	0.300	0.300	0.300
f [m]	0.600	0.600	0.600	0.600	0.600	0.600
g [m]	0.600	0.600	0.600	0.600	0.600	0.600
Truss section type	K12_F2-0	K12_F2-0	K12_F2-0	K12_F2-0	K12_F2-0	K12_F2-0
Truss section thickness [mm]	8	8	8	8	8	8
Truss section type [mm]	0.75	0.75	0.75	0.75	0.75	0.75
Web type	K12_F2-0					
Width [mm]	780					
Truss section [mm]	14					
Web height [mm]	10					
Web width [mm]	82					
Web height [mm]	10					
Web width [mm]	82					
Web type [mm]	0.5					



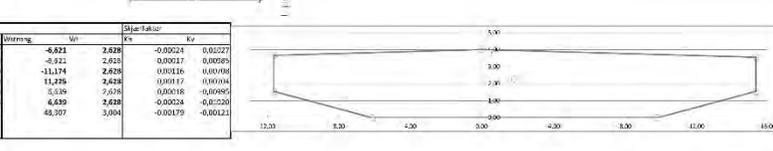
Top height					
HTP (to Pier) [m]	-2.832				
VTP (to L1) [m]	2.267				
HTP (to L1) [m]	2.251				
VTP (to L1) [m]	2.245				

Effort	7.85	2/m
Force	2.50E+05	N/m
Position	0.3	
Coordinate	8.00E+04	N/m

Section	01.074 m2
Area	2.891 m2
Perimeter, no LK	1.201 m
Perimeter, no LK	2.251 m
Perimeter, no LK	0.422 m
Perimeter, no LK	0.911 m
Perimeter, no LK	0.780 m
Perimeter, no LK	2.781 m
Perimeter, no LK	2.428 m
Perimeter, no LK	2.888 m
Perimeter, no LK	89.591 m
Perimeter, no LK	1341.438 m
Mass	10.64 t
Mass	2.00 t
Mass	12.89 t
Mass	0.74 t
Mass	4.62 t
Mass	17.78 t
Mass	1.09 t
Mass	19.00 t



Point	Y	Z	Mx	My	Mz	Vx	Vy	Vz
Punkt C, topp øst	-15.304	3.553	0.014	-2.154	2.875	2.817	-6.922	2.628
Punkt C, bunn øst	-15.389	3.516	0.014	-2.091	2.807	-6.922	2.628	
Punkt D, bunn øst	-9.850	0.000	0.014	-1.228	-1.850	-11.174	2.628	
Punkt A, bunn vest	6.168	0.000	0.014	-1.228	-1.850	11.276	2.628	
Punkt E	11.664	1.564	0.014	-1.844	-2.808	5.138	2.628	
Punkt B, topp vest	31.644	3.664	0.014	1.984	2.594	6.439	2.628	
Punkt B'	0.000	0.014	-0.015	1.587	1.976	48.397	3.084	



| Effective slenderness ratio for buckling |
|--|--|--|--|
| Aeff,C | 3.040 m2 | | |
| Aeff,T | 2.331 m2 | | |
| Ww,N,C | -0.071 m | | |
| Ww,N,T | 0.000 m | | |
| Ww,N,C | -0.015 m | | |
| Ww,N,T | 0.000 m | | |
| Ww,weak,off | 1.198 m3 | | |
| Ww,weak,off | -1.054 m3 | | |
| Ww,strong,off | 5.583 m3 | | |
| Ww,strong,off | 5.583 m3 | | |

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| Aeff,C | 3.040 m2 | | |
| Aeff,T | 2.331 m2 | | |
| Ww,N,C | -0.071 m | | |
| Ww,N,T | 0.000 m | | |
| Ww,N,C | -0.015 m | | |
| Ww,N,T | 0.000 m | | |
| Ww,weak,off | 1.198 m3 | | |
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| Ww,strong,off | 5.583 m3 | | |

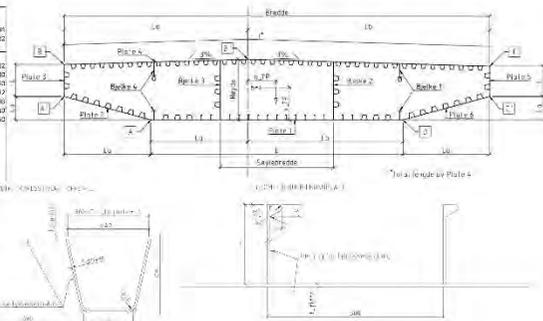
Reduction factors	Plate 1	Plate 2	Plate 3	Plate 4	Plate 5	Plate 6
Reduction factors						
Reduction factors						
Reduction factors						
Reduction factors						
Reduction factors						
Reduction factors						

Reduction factors	Plate 1	Plate 2	Plate 3	Plate 4	Plate 5	Plate 6
Reduction factors						
Reduction factors						
Reduction factors						
Reduction factors						
Reduction factors						
Reduction factors						

Concept development, floating bridge E39 Bjørnafjord

K12 02

Property	Plate 1	Plate 2	Plate 3	Plate 4	Plate 5	Plate 6
Area [m²]	22	22	30	30	32	32
Perimeter [m]	116,00	116,00	150,00	150,00	143,00	143,00
Volume [m³]	116,00	116,00	150,00	150,00	143,00	143,00
Mass [kg]	116,00	116,00	150,00	150,00	143,00	143,00
Centroid X [m]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Y [m]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Z [m]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Ix [m⁴]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Iy [m⁴]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Iz [m⁴]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Ixy [m⁴]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Iyz [m⁴]	0,00	0,00	0,00	0,00	0,00	0,00
Centroid Ixz [m⁴]	0,00	0,00	0,00	0,00	0,00	0,00

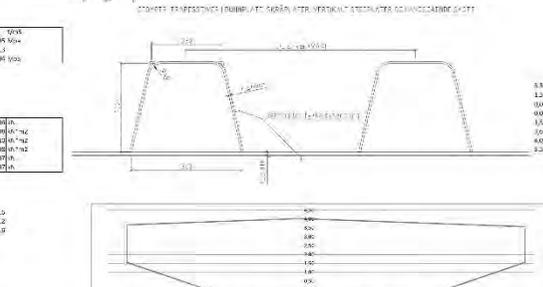


Property	Value
Area [m²]	0,013 m
Perimeter [m]	0,000 m
Volume [m³]	0,000 m
Mass [kg]	0,000 m

Property	Value
Area [m²]	7,88 m²
Perimeter [m]	2,307 m
Volume [m³]	0,000 m
Mass [kg]	0,000 m

Property	Value
Area [m²]	1,000 m²
Perimeter [m]	2,000 m
Volume [m³]	1,000 m³
Mass [kg]	1,000 kg
Centroid X [m]	0,000 m
Centroid Y [m]	0,000 m
Centroid Z [m]	0,000 m
Centroid Ix [m⁴]	0,000 m⁴
Centroid Iy [m⁴]	0,000 m⁴
Centroid Iz [m⁴]	0,000 m⁴
Centroid Ixy [m⁴]	0,000 m⁴
Centroid Iyz [m⁴]	0,000 m⁴
Centroid Ixz [m⁴]	0,000 m⁴

Property	Value
Area [m²]	1,000 m²
Perimeter [m]	2,000 m
Volume [m³]	1,000 m³
Mass [kg]	1,000 kg
Centroid X [m]	0,000 m
Centroid Y [m]	0,000 m
Centroid Z [m]	0,000 m
Centroid Ix [m⁴]	0,000 m⁴
Centroid Iy [m⁴]	0,000 m⁴
Centroid Iz [m⁴]	0,000 m⁴
Centroid Ixy [m⁴]	0,000 m⁴
Centroid Iyz [m⁴]	0,000 m⁴
Centroid Ixz [m⁴]	0,000 m⁴



Property	Value
Area [m²]	1,000 m²
Perimeter [m]	2,000 m
Volume [m³]	1,000 m³
Mass [kg]	1,000 kg
Centroid X [m]	0,000 m
Centroid Y [m]	0,000 m
Centroid Z [m]	0,000 m
Centroid Ix [m⁴]	0,000 m⁴
Centroid Iy [m⁴]	0,000 m⁴
Centroid Iz [m⁴]	0,000 m⁴
Centroid Ixy [m⁴]	0,000 m⁴
Centroid Iyz [m⁴]	0,000 m⁴
Centroid Ixz [m⁴]	0,000 m⁴

Property	Value
Area [m²]	1,000 m²
Perimeter [m]	2,000 m
Volume [m³]	1,000 m³
Mass [kg]	1,000 kg
Centroid X [m]	0,000 m
Centroid Y [m]	0,000 m
Centroid Z [m]	0,000 m
Centroid Ix [m⁴]	0,000 m⁴
Centroid Iy [m⁴]	0,000 m⁴
Centroid Iz [m⁴]	0,000 m⁴
Centroid Ixy [m⁴]	0,000 m⁴
Centroid Iyz [m⁴]	0,000 m⁴
Centroid Ixz [m⁴]	0,000 m⁴

Property	Value
Area [m²]	1,000 m²
Perimeter [m]	2,000 m
Volume [m³]	1,000 m³
Mass [kg]	1,000 kg
Centroid X [m]	0,000 m
Centroid Y [m]	0,000 m
Centroid Z [m]	0,000 m
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Centroid Iy [m⁴]	0,000 m⁴
Centroid Iz [m⁴]	0,000 m⁴
Centroid Ixy [m⁴]	0,000 m⁴
Centroid Iyz [m⁴]	0,000 m⁴
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Property	Value
Area [m²]	1,000 m²
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Volume [m³]	1,000 m³
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Centroid Ixy [m⁴]	0,000 m⁴
Centroid Iyz [m⁴]	0,000 m⁴
Centroid Ixz [m⁴]	0,000 m⁴